Writing Products as Sums and Sums as Products

1. Write the expression below in standard form.

$$3h - 2(1 + 4h)$$

2. Write the expression below as a product of two factors.

$$6m + 8n + 4$$

1. Write each expression as the product of two factors.

a.
$$1 \cdot 3 + 7 \cdot 3$$

b.
$$(1+7)+(1+7)+(1+7)$$

c.
$$2 \cdot 1 + (1+7) + (7 \cdot 2)$$

d.
$$h \cdot 3 + 6 \cdot 3$$

e.
$$(h+6)+(h+6)+(h+6)$$

f.
$$2h + (6+h) + 6 \cdot 2$$

g.
$$j \cdot 3 + k \cdot 3$$

h.
$$(j + k) + (j + k) + (j + k)$$

i.
$$2i + (k+i) + 2k$$

2. Write each sum as a product of two factors.

a.
$$6 \cdot 7 + 3 \cdot 7$$

b.
$$(8+9)+(8+9)+(8+9)$$

c.
$$4 + (12 + 4) + (5 \cdot 4)$$

d.
$$2y \cdot 3 + 4 \cdot 3$$

e.
$$(x+5)+(x+5)$$

f.
$$3x + (2 + x) + 5 \cdot 2$$

g.
$$f \cdot 6 + g \cdot 6$$

h.
$$(c+d)+(c+d)+(c+d)+(c+d)$$

i.
$$2r + r + s + 2s$$

3. Use the following rectangular array to answer the questions below.

	?	5	?
?	15f	5g	45

- Fill in the missing information.
- b. Write the sum represented in the rectangular array.
- Use the missing information from part (a) to write the sum from part (b) as a product of two factors. c.
- Write the sum as a product of two factors.

a.
$$81w + 48$$

b.
$$10 - 25t$$

c.
$$12a + 16b + 8$$

- 5. Xander goes to the movies with his family. Each family member buys a ticket and two boxes of popcorn. If there are five members of his family, let t represent the cost of a ticket and p represent the cost of a box of popcorn. Write two different expressions that represent the total amount his family spent. Explain how each expression describes the situation in a different way.
- 6. Write each expression in standard form.

a.
$$-3(1-8m-2n)$$

b.
$$5 - 7(-4q + 5)$$

c.
$$-(2h-9)-4h$$

d.
$$6(-5r-4)-2(r-7s-3)$$

7. Combine like terms to write each expression in standard form.

a.
$$(r-s) + (s-r)$$

b.
$$(-r+s)+(s-r)$$

c.
$$(-r-s)-(-s-r)$$

d.
$$(r-s) + (s-t) + (t-r)$$

e.
$$(r-s)-(s-t)-(t-r)$$

Write the expression below in standard form.

$$3h - 2(1 + 4h)$$

$$3h + (-2(1+4h))$$

Subtraction as adding the inverse

$$3h + (-2 \cdot 1) + (-2h \cdot 4)$$

Distributive property

$$3h + (-2) + (-8h)$$

Apply integer rules

$$-5h - 2$$

Collect like terms

2. Write the expression below as a product of two factors.

6m + 8n + 4

The GCF for the terms is 2. Therefore, the factors are 2(3m + 4n + 2).

Write each expression as the product of two factors.

a.
$$1 \cdot 3 + 7 \cdot 3$$

b.
$$(1+7)+(1+7)+(1+7)$$

$$3(1+7)$$

$$3(1 + 7)$$

d.
$$h \cdot 3 + 6 \cdot 3$$

e.
$$(h+6)+(h+6)+(h+6)$$

f.
$$2h + (6+h) + 6 \cdot 2$$

c. $2 \cdot 1 + (1+7) + (7 \cdot 2)$

$$3(h + 6)$$

$$3(h+6)$$

$$3(h+6)$$

g.
$$j \cdot 3 + k \cdot 3$$

i.
$$2j + (k+j) + 2k$$

 $3(j+k)$

$$3(j+k)$$
 $3(j+k)$

2. Write each sum as a product of two factors.

a.
$$6 \cdot 7 + 3 \cdot 7$$

b.
$$(8+9)+(8+9)+(8+9)$$
 c. $4+(12+4)+(5\cdot4)$

h. (j + k) + (j + k) + (j + k)

$$7(6+3)$$

$$3(8+9)$$

$$4(1+4+5)$$

d.
$$2y \cdot 3 + 4 \cdot 3$$

e.
$$(x+5)+(x+5)$$

f.
$$3x + (2 + x) + 5 \cdot 2$$

$$3(2y + 4)$$

$$2(x + 5)$$

$$4(x+3)$$

g.
$$f \cdot 6 + g \cdot 6$$

h.
$$(c+d)+(c+d)+(c+d)+(c+d)$$

i.
$$2r+r+s+2s$$

$$6(f + g)$$

$$4(c + d)$$

$$3(r+s)$$

Use the following rectangular array to answer the questions below.

	5	5	?	
?	15f	5g	45	

Fill in the missing information.

	3 <i>f</i>	<i>g</i> ?	9 ?	
5 ?	15f	5g	45	

Write the sum represented in the rectangular array.

$$15f + 5g + 45$$

Use the missing information from part (a) to write the sum from part (b) as a product of two factors.

$$5(3f + g + 9)$$

Write the sum as a product of two factors.

a.
$$81w + 48$$

$$3(27w + 16)$$

b.
$$10 - 25t$$

$$5(2-5t)$$

c.
$$12a + 16b + 8$$

$$4(3a+4b+2)$$

Xander goes to the movies with his family. Each family member buys a ticket and two boxes of popcorn. If there are five members of his family, let t represent the cost of a ticket and p represent the cost of a box of popcorn. Write two different expressions that represent the total amount his family spent. Explain how each expression describes the situation in a different way.

$$5(t + 2p)$$

Five people each buy a ticket and two boxes of popcorn, so the cost is five times the quantity of a ticket and two boxes of popcorn.

$$5t + 10p$$

There are five tickets and 10 boxes of popcorn total. The total cost will be five times the cost of the tickets, plus 10 times the cost of the popcorn.

6. Write each expression in standard form.

a.
$$-3(1-8m-2n)$$

$$-3(1+(-8m)+(-2n))$$

$$-3 + 24m + 6n$$

b.
$$5 - 7(-4q + 5)$$

$$5 + -7(-4q + 5)$$

$$5 + 28q + -35$$

$$28q - 35 + 5$$

$$28q - 30$$

c.
$$-(2h-9)-4h$$

$$-(2h+(-9))+(-4h)$$

$$-2h + 9 + (-4h)$$

$$-6h + 9$$
 or $9 - 6h$

d.
$$6(-5r-4)-2(r-7s-3)$$

$$6(-5r+-4)+-2(r-7s+-3)$$

$$-30r + -24 + -2r + 14s + 6$$

$$-30r + -2r + 14s + -24 + 6$$

$$-32r + 14s - 18$$

7. Combine like terms to write each expression in standard form.

a.
$$(r-s) + (s-r)$$

0

b.
$$(-r+s)+(s-r)$$

$$-2r + 2s$$

c.
$$(-r-s)-(-s-r)$$

0

d.
$$(r-s) + (s-t) + (t-r)$$

0

e.
$$(r-s)-(s-t)-(t-r)$$

$$2r-2s$$