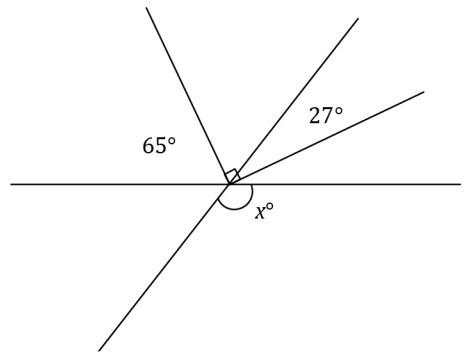
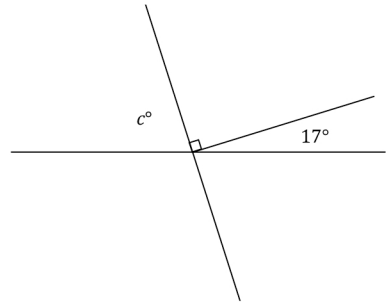


## Solving for Unknown Angles Using Equations

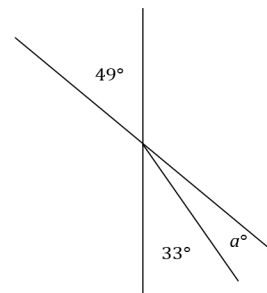
Set up and solve an equation to find the value of  $x$ . Explain why your answer is reasonable.



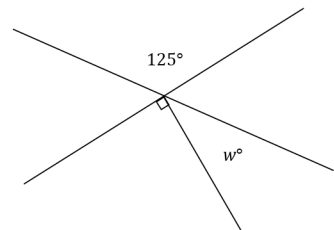
1. Two lines meet at the vertex of a ray. Set up and solve an equation to find the value of  $c$ .



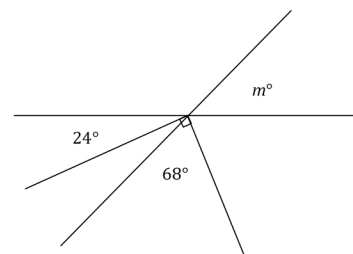
2. Two lines meet at the vertex of a ray. Set up and solve an equation to find the value of  $a$ . Explain why your answer is reasonable.



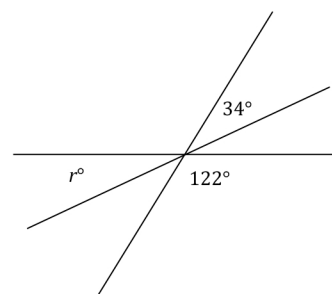
3. Two lines meet at the vertex of a ray. Set up and solve an equation to find the value of  $w$ .



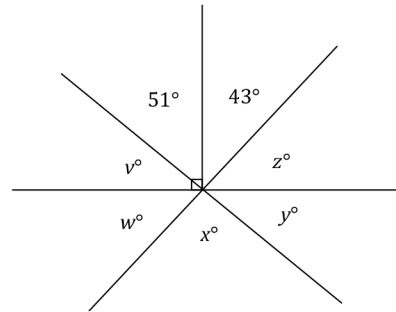
4. Two lines meet at the common vertex of two rays. Set up and solve an equation to find the value of  $m$ .



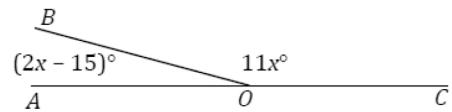
5. Three lines meet at a point. Set up and solve an equation to find the value of  $r$ .



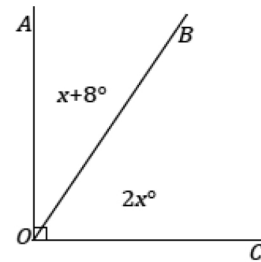
6. Three lines meet at the vertex of a ray. Set up and solve an equation to find the value of each variable in the diagram.



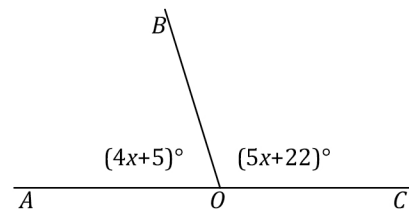
7. Set up and solve an equation to find the value of  $x$ . Find the measurement of  $\angle AOB$  and of  $\angle BOC$ .



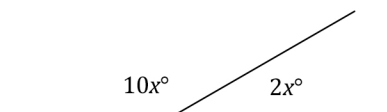
8. Set up and solve an equation to find the value of  $x$ . Find the measurement of  $\angle AOB$  and of  $\angle BOC$ .



9. Set up and solve an equation to find the value of  $x$ . Find the measurement of  $\angle AOB$  and of  $\angle BOC$ .



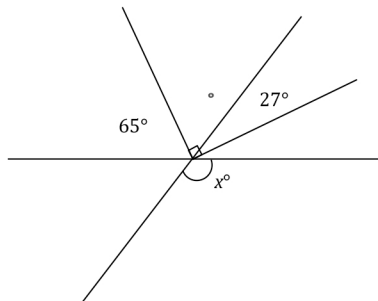
10. Write a verbal problem that models the following diagram. Then solve for the two angles.



Set up and solve an equation to find the value of  $x$ . Explain why your answer is reasonable.

There are multiple solutions to the problem. Two possible solutions are shown below.

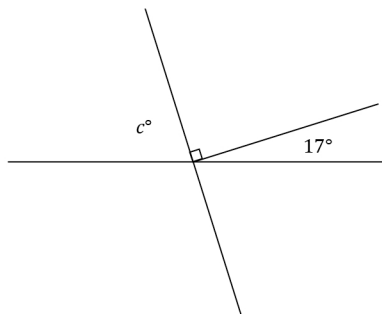
or



The answers seem reasonable because a rounded value of  $x$  as  $17^\circ$  and a rounded value of its adjacent angle as  $63^\circ$ , yields a sum of  $80^\circ$ , which is close to the calculated answer.

1. Two lines meet at the vertex of a ray. Set up and solve an equation to find the value of  $c$ .

on a line



Scaffolding:

Students struggling to organize their solution may benefit from prompts such as the following: Write an equation to model this situation. Explain how your equation describes the situation. Solve and interpret the solution. Is it reasonable?

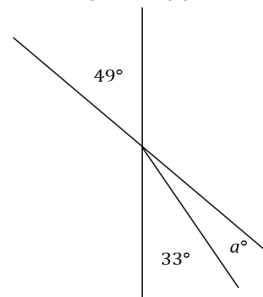
Scaffolded solutions:

- Use equation above.
- The angle marked  $c$ , the right angle, and the angle with measurement  $17$  are angles on a line and their measurements sum to  $180$ .
- Use solution above. The answer seems reasonable because it looks like it has a measurement a little less than a  $90$  angle.

2. Two lines meet at the vertex of a ray. Set up and solve an equation to find the value of  $a$ . Explain why your answer is reasonable.

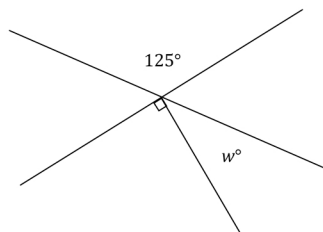
add and vert

The answers seem reasonable because a rounded value of  $a$  as  $49$  and a rounded value of its adjacent angle as  $33$ , yields a sum of  $82$ , which is close to the rounded value of the measurement of the vertical angle.



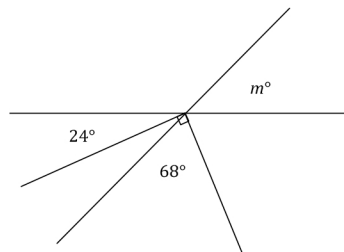
3. Two lines meet at the vertex of a ray. Set up and solve an equation to find the value of  $w$ .

*add and vert*



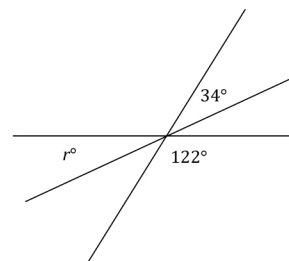
4. Two lines meet at the common vertex of two rays. Set up and solve an equation to find the value of  $m$ .

*add and vert*



5. Three lines meet at a point. Set up and solve an equation to find the value of  $r$ .

*on a line and vert*



6. Three lines meet at the vertex of a ray. Set up and solve an equation to find the value of each variable in the diagram.

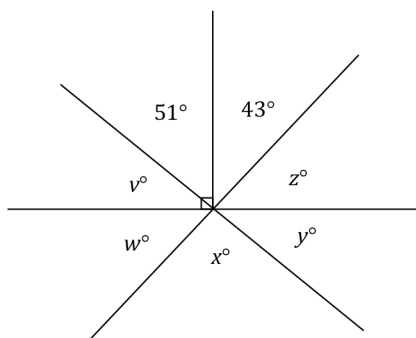
*complementary*

*on a line*

*vert*

*vert*

*vert*

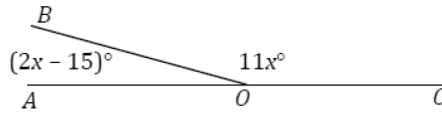


7. Set up and solve an equation to find the value of  $x$ . Find the measurement of  $y$  and of  $z$ .

**Scaffolding:**

Students struggling to organize their solution may benefit from prompts such as the following:

- Write an equation to model this situation. Explain how your equation describes the situation. Solve and interpret the solution. Is it reasonable?



supplementary

The measurement of  
The measurement of

Scaffolded solutions:

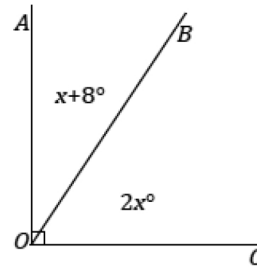
- Use equation above.
- The marked angles are angles on a line and their measurements sum to .
- The answers seem reasonable because once is substituted, the respective angle measurements seem appropriate since is acute and is obtuse.

8. Set up and solve an equation to find the value of . Find the measurement of and of .

complementary

The measurement of - -

The measurement of - -



9. Set up and solve an equation to find the value of . Find the measurement of

on a line

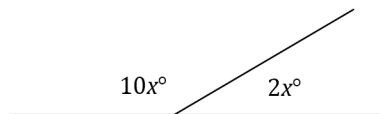
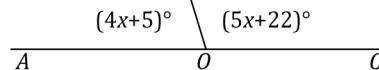
The measurement of

The measurement of

10. Write a verbal problem that models the following diagram. Then solve for the two angles.

One possible response: Two angles are supplementary. The measurement of one angle is five times the other. Find the measurements of both angles.

on a line



The measurement of Angle 1:

The measurement of Angle 2: