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Operations with Numbers in Scientific Notation

1. The speed of light is 3×10^8 meters per second. The sun is approximately 230,000,000,000 meters from Mars. How many seconds does it take for sunlight to reach Mars?

2. If the sun is approximately 1.5×10^{11} meters from Earth, what is the approximate distance from Earth to Mars?

- 1. The sun produces 3.8×10^{27} joules of energy per second. How much energy is produced in a year? (Note: a year is approximately 31,000,000 seconds).
- 2. On average, Mercury is about 57,000,000 km from the sun, whereas Neptune is about 4.5×10^9 km from the sun. What is the difference between Mercury's and Neptune's distances from the sun?
- 3. The mass of Earth is approximately 5.9×10^{24} kg, and the mass of Venus is approximately 4.9×10^{24} kg.
 - Find their combined mass.
 - Given that the mass of the sun is approximately 1.9×10^{30} kg, how many Venuses and Earths would it take to equal the mass of the sun?

The speed of light is 3×10^8 meters per second. The sun is approximately 230,000,000,000 meters from Mars. How many seconds does it take for sunlight to reach Mars?

$$230,000,000,000 = 2.3 \times 10^{11}$$

$$\frac{2.3 \times 10^{11}}{3 \times 10^{8}} = \frac{2.3}{3} \times \frac{10^{11}}{10^{8}}$$

$$= 0.76 ... \times 10^{3}$$

$$\approx 0.76 \times 10 \times 10^{2}$$

$$\approx 7.6 \times 10^{2}$$

It takes approximately 760 seconds for sunlight to reach Mars.

If the sun is approximately 1.5×10^{11} meters from Earth, what is the approximate distance from Earth to Mars?

$$2.3 \times 10^{11} - 1.5 \times 10^{11} = 2.3 - 1.5 \times 10^{11}$$

$$= 0.8 \times 10^{11}$$

$$= 0.8 \times 10 \times 10^{10}$$

$$= 8 \times 10^{10}$$

The distance from Earth to Mars is 8×10^{10} meters.

Students practice operations with numbers written in scientific notation and standard notation.

The sun produces 3.8×10^{27} joules of energy per second. How much energy is produced in a year? (Note: a year is approximately 31,000,000 seconds).

$$31,000,000 = 3.1 \times 10^{7}$$

$$3.8 \times 10^{27} \quad 3.1 \times 10^{7} = 3.8 \times 3.1 \quad 10^{27} \times 10^{7}$$

$$= 11.78 \times 10^{34}$$

$$= 1.178 \times 10 \times 10^{34}$$

$$= 1.178 \times 10^{35}$$

The sun produces 1.178×10^{35} joules of energy in a year.

On average, Mercury is about 57,000,000 km from the sun, whereas Neptune is about 4.5×10^9 km from the sun. What is the difference between Mercury's and Neptune's distances from the sun?

$$57,000,000 = 5.7 \times 10^{7}$$

$$4.5 \times 10^{9} - 5.7 \times 10^{7} = 4.5 \times 10^{2} \times 10^{7} - 5.7 \times 10^{7}$$

$$= 450 \times 10^{7} - 5.7 \times 10^{7}$$

$$= 450 - 5.7 \times 10^{7}$$

$$= 444.3 \times 10^{7}$$

$$= 4.443 \times 10^{2} \times 10^{7}$$

$$= 4.443 \times 10^{9}$$

The difference in the distance of Mercury and Neptune from the sun is $4.443\times10^9\,\text{km}.$

- The mass of Earth is approximately 5.9×10^{24} kg, and the mass of Venus is approximately 4.9×10^{24} kg.
 - Find their combined mass.

$$\begin{aligned} 5.9 \times 10^{24} + 4.9 \times 10^{24} &= 5.9 + 4.9 \times 10^{24} \\ &= 10.8 \times 10^{24} \\ &= 1.08 \times 10 \times 10^{24} \\ &= 1.08 \times 10^{25} \end{aligned}$$

The combined mass of Earth and Venus is 1.08×10^{25} kg.

Given that the mass of the sun is approximately 1.9×10^{30} kg, how many Venuses and Earths would it take to equal the mass of the sun?

$$\begin{split} \frac{1.9\times10^{30}}{1.08\times10^{25}} &= \frac{1.9}{1.08}\times\frac{10^{30}}{10^{25}}\\ &= 1.75925...\times10^{5}\\ &\approx 1.8\times10^{5} \end{split}$$

It would take approximately 1.8×10^5 Venuses and Earths to equal the mass of the sun.